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## PolSAR image classification using a semi-supervised classifier based on hypergraph learning

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This letter presents a novel semi-supervised method based on hypergraph learning for polarimetric synthetic aperture radar (PolSAR) image classification. Compared with the classic support vector machine, simple-graph learning,  $k$ -nearest neighbour ( $k$ -NN) and semi-supervised discriminant analysis (SDA) classifiers, the proposed method achieves better performance with fewer labelled points for PolSAR imagery. A hyper-spectral image is used for comparison with use of PolSAR imagery, and the proposed method is found to be inferior to  $k$ -NN and SDA for the hyperspectral image. The performance of our method is evaluated in single, dual and full-polarization cases, respectively. The results demonstrate that the performance of our method in the full-polarization case is superior to that in either single or dual-polarization case.

### 1. Introduction

Currently, there is widespread interest in the development of polarimetric synthetic aperture radar (PolSAR) for earth observation because of its all-weather day and night capabilities. How to accurately and robustly classify PolSAR imagery is one of the most active research topics nowadays. Several classification algorithms have been developed in recent years, including expectation-maximization (Beaulieu and Touzi 2004), support vector machines (SVMs) (Lardeux et al. 2009), spectral graph partitioning (Ersahin, Cumming, and Ward 2010), wavelet texture models (De Grandi, Lee, and Schuler 2007), etc. In general, PolSAR classification algorithms can be characterized as supervised, semi-supervised or unsupervised, according to whether there is training data to participate in learning. PolSAR classification algorithms also can be characterized according to methods based on target decomposition or statistical property by feature expression.

In supervised classification, training data sets for each class are selected based on reference data maps or scattering contrast differences in PolSAR imagery. The unsupervised classification method classifies images automatically by locating clusters based on a specific criterion. The final class identification must be inferred manually (Lee and Pottier 2009). The misclassification ratio is more difficult to define. The semi-supervised method is a compromise between the supervised and unsupervised methods. Supervised classification for SAR data usually encounters a problem of time consumption and it is costly to obtain the reference data; unsupervised classification encounters trouble locating the final class identification. Therefore, the highly desirable method is the one that achieves better performance with fewer training samples, without the trouble of locating the final class

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identification. For PolSAR classification, the emphasis is on the latter taxonomy. For the method based on target decomposition, each class is determined by diverse after-scattering and polarization features. For the method based on a statistical property, the featured expression for training and testing data is extracted from the statistical property.

In this letter, we focus on the semi-supervised classification method and develop a novel method based on hypergraph learning (HGL) (Zhou, Huang, and Scholkopf 2006; Agarwal, Branson, and Belongie 2006; Huang et al. 2010; Yu, Rui, and Tao 2014; Yu et al. 2014; Yu, Rui, and Chen 2014). Our proposed method is a general transductive learning method (Wu and Scholkopf 2007) that explores labelled and unlabelled data simultaneously (Yu et al. 2011). Our method regularizes the hyperedge weights and optimizes the labels and hyperedge weights simultaneously.

## 2. Method

### 2.1. Feature description

In this letter, we describe a two-step feature. The first step is derived from Pauli decomposition; the second takes into account speckle reduction.

Because its physical meaning is explicit, target decomposition is the main method used to extract features from PolSAR data. Thus, much research is devoted to target decomposition. The simple case is that of Pauli decomposition:

$$\mathbf{x} = (|S_{hh} + S_{vv}| \quad |S_{hh} - S_{vv}| \quad 2|S_{hv}|)^T, \quad (1)$$

where  $S_{pq}$  denotes the scattering matrix element corresponding to the  $pq$  polarization of a receiving–transmitting wave ( $p$  and  $q$  referring to horizontal  $h$  or vertical  $v$  linear polarization); the notation  $|\cdot|$  denotes the amplitude of the wave after scattering; the superscript  $T$  denotes matrix transposition, and the notation  $\mathbf{x}$  is a PolSAR feature vector.  $S_{hv}$  is equal to  $S_{vh}$  for reciprocity in most cases according to Pauli decomposition.

Then, we set that,  $\mathbf{x}_s$ ,  $\mathbf{x}_d$ ,  $\mathbf{x}_f$  are the feature vectors of single-polarization, dual-polarization and full-polarization, respectively, as follows:

$$\begin{aligned} \mathbf{x}_f &= (\langle |S_{hh} + S_{vv}| \rangle \quad \langle |S_{hh} - S_{vv}| \rangle \quad 2\langle |S_{hv}| \rangle)^T \\ \mathbf{x}_d &= (\langle |S_{hh}| \rangle \quad \langle |S_{vv}| \rangle)^T \\ \mathbf{x}_s &= (\langle |S_{hh}| \rangle \quad \langle |S_{vv}| \rangle) \end{aligned}, \quad (2)$$

where the notation  $\langle \cdot \rangle$  stands for the spatial averaging over a  $3 \times 3$  (or other size) neighbourhood. Speckle appearance in SAR images is due to the coherent interference of waves reflected from many elementary scatters. This effect causes a pixel-to-pixel variation in intensities, and the variation manifests itself as a granular noise pattern in SAR images. Speckles reduce the image classification accuracy. Here, we take simple averaging to reduce the speckle noise (Lee, Grunes, and De Grandi 1999).

### 2.2. Hypergraph learning

We start from a simple graph whose vertices represent samples, and each edge connects two related vertices. The simple graph denotes pairwise relationships and is created based upon pairwise distance. We classify samples with graph-based learning in a feature space.

However, simple graph learning (SGL) fails to capture high-order information, such as the information of clustering, which causes the development of hypergraph learning (HGL). A hyperedge in a hypergraph links several (two or more) vertices that show the clustering information.

A brief description of the hypergraph construction is introduced. Given  $c$  categories of PolSAR image, including  $m$  training PolSAR image points  $(\mathbf{x}_1, \mathbf{y}_1), \dots, (\mathbf{x}_m, \mathbf{y}_m)$  and  $n$  testing data points  $(\mathbf{x}_{m+1}, \mathbf{0}), \dots, (\mathbf{x}_{m+n}, \mathbf{0})$ , where  $\mathbf{x}_i \in \mathbb{R}^d, 1 \leq i \leq m+n$  is the input space;  $\mathbf{y}_i = [0, \dots, 1, \dots, 0]^T \in \mathbb{R}^{c \times 1}, 1 \leq i \leq m$  is the label vector of  $\mathbf{x}_i$ , where the  $g$ th component is 1 if  $\mathbf{x}_i$  belongs to the  $g$ th category, otherwise, 0; and  $\mathbf{0}$  is a vector with  $c$  components 0.

The hypergraph,  $\mathbf{H} = (\mathbf{x}, \boldsymbol{\varepsilon})$ , is formed by the vertex set,  $\mathbf{x}$ , and the hyperedge set,  $\boldsymbol{\varepsilon}$ . An incidence matrix,  $\mathbf{A}$ , whose size is  $|\mathbf{x}| \times |\boldsymbol{\varepsilon}|$ , denotes the hypergraph with the following elements:

$$\mathbf{A}(i, j) = \begin{cases} 1, & \text{if } \mathbf{x}_i \in \boldsymbol{\varepsilon}_j \\ 0, & \text{if } \mathbf{x}_i \notin \boldsymbol{\varepsilon}_j \end{cases}, \quad (3)$$

where  $\boldsymbol{\varepsilon}_j$  denotes the  $j$ th subset of the hyperedge set. The distance between two data points is

$$\begin{aligned} \text{dist}(\mathbf{x}_i, \mathbf{x}_j) &= \exp\left(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{\sigma^2}\right) \\ \sigma &= \sqrt{\frac{1}{m+n-1} \sum_{\delta=1}^{m+n} \|\mathbf{x}_\delta - \bar{\mathbf{x}}\|^2} \quad \bar{\mathbf{x}} = \frac{1}{m+n} \sum_{\delta=1}^{m+n} \mathbf{x}_\delta \end{aligned} \quad (4)$$

We use  $\boldsymbol{\varphi}$ ,  $\boldsymbol{\gamma}$  and  $\boldsymbol{\omega}$  to denote diagonal matrices of vertex degrees, hyperedge degrees and hyperedge weights, respectively.  $\boldsymbol{\varphi}_i$  denotes the entry  $(i, i)$  of matrix  $\boldsymbol{\varphi}$ ;  $\boldsymbol{\omega}_i$  and  $\boldsymbol{\gamma}_i$  have similar meanings. Then, the initial weight,  $\boldsymbol{\omega}_i$ , is

$$\boldsymbol{\omega}_i = \sum_{\mathbf{x}_j \in \boldsymbol{\varepsilon}_i} \text{dist}(\mathbf{x}_i, \mathbf{x}_j). \quad (5)$$

Based on  $\mathbf{A}$ , the  $i$ th vertex degree,  $\boldsymbol{\varphi}_i$ , is

$$\boldsymbol{\varphi}_i = \sum_{\boldsymbol{\varepsilon}_j \in \boldsymbol{\varepsilon}} \boldsymbol{\omega}_j \mathbf{A}(i, j), \quad (6)$$

and the  $i$ th hyperedge degree,  $\boldsymbol{\gamma}_i$ , is

$$\boldsymbol{\gamma}_i = \sum_{\mathbf{x}_j \in \mathbf{x}} \mathbf{A}(j, i). \quad (7)$$

In this letter, we adopt the regularization framework proposed in Yu, Tao, and Wang (2012), i.e.,

$$\begin{aligned} & \arg \min_{\mathbf{F}, \boldsymbol{\omega}} \sum_{\eta=1}^c \left( \mathbf{f}_{\eta}^T \mathbf{L} \mathbf{f}_{\eta} \right) + \lambda \|\mathbf{f}_{\eta} - \mathbf{Y}_{\eta}\|^2 + \mu \|\text{diag}(\boldsymbol{\omega})\|^2 \\ & \text{s.t. } \sum_{j=1}^l \boldsymbol{\omega}_j = 1, \boldsymbol{\omega}_j \geq 0, j=1, \dots, l \end{aligned} \quad (8)$$

where  $\mathbf{L} = \mathbf{I} - \boldsymbol{\Phi}^{-(1/2)} \mathbf{A} \boldsymbol{\Gamma}^{-1} \boldsymbol{\omega} \mathbf{A}^T \boldsymbol{\Phi}^{-(1/2)}$ ;  $l$  is the number of hyperedges;  $\text{diag}(\boldsymbol{\omega})$  is the diagonal vector of  $\boldsymbol{\omega}$ , i.e.,  $(\boldsymbol{\omega}_1, \boldsymbol{\omega}_2, \dots, \boldsymbol{\omega}_l)$ ;  $c$  is the number of classes;  $\mathbf{F}$  is a matrix,  $\mathbf{F} = (\mathbf{f}_1, \dots, \mathbf{f}_c) \in \mathbb{R}^{(m+n) \times c}$ ,  $\mathbf{f}_{\eta}$  is the classification function for the data belonging to the  $\eta$ th category;  $\lambda > 0$  and  $\mu > 0$  are two trade-off parameters to balance the empirical loss, the weight and the regularization;  $\mathbf{Y} = (\mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_m, \mathbf{0}, \dots, \mathbf{0})^T$ ,  $\mathbf{Y} \in \mathbb{R}^{(m+n) \times c}$ ,  $\mathbf{Y}_{\eta}$  is the  $\eta$ th column of  $\mathbf{Y}$ . The third term is introduced to avoid a degenerate solution caused by the former two terms existing only in the regularization. Here we add two constraints, one to fix the summation of the weights,  $\sum_{j=1}^l \boldsymbol{\omega}_j = 1$  and one to avoid negative weights,  $\boldsymbol{\omega}_j \geq 0$

Because the classifier function is not jointly convex with respect to  $\mathbf{F}$  and  $\boldsymbol{\omega}$ , we solve one variable by fixing another variable.

First we initialize  $\boldsymbol{\omega}$  with Equation (6), so the solution of  $\mathbf{F}$  becomes

$$\mathbf{F} = \frac{\lambda}{\lambda + 1} \left( \mathbf{I} - \frac{\boldsymbol{\Phi}^{-(1/2)} \mathbf{A} \boldsymbol{\Gamma}^{-1} \boldsymbol{\omega} \mathbf{A}^T \boldsymbol{\Phi}^{-(1/2)}}{1 + \lambda} \right)^{-1} \mathbf{Y}. \quad (9)$$

Then we update the weights,  $\boldsymbol{\omega}$ , with an iterative coordinate descent method as follows:

$$\begin{cases} \boldsymbol{\omega}_i^{t+1} = 0, \boldsymbol{\omega}_j^{t+1} = \boldsymbol{\omega}_i^t + \boldsymbol{\omega}_j^t, & \text{if } 2\mu(\boldsymbol{\omega}_i^t + \boldsymbol{\omega}_j^t) + (s_j - s_i) \leq 0 \\ \boldsymbol{\omega}_i^{t+1} = \boldsymbol{\omega}_i^t + \boldsymbol{\omega}_j^t, \boldsymbol{\omega}_j^{t+1} = 0, & \text{if } 2\mu(\boldsymbol{\omega}_i^t + \boldsymbol{\omega}_j^t) + (s_i - s_j) \leq 0 \\ \boldsymbol{\omega}_i^{t+1} = \frac{2\mu(\boldsymbol{\omega}_i^t + \boldsymbol{\omega}_j^t) + (s_j - s_i)}{4\mu}, \boldsymbol{\omega}_j^{t+1} = \boldsymbol{\omega}_i^t + \boldsymbol{\omega}_j^t - \boldsymbol{\omega}_i^{t+1}, & \text{otherwise} \end{cases} \quad (10)$$

where  $s_i = \sum_{z=1}^c -(\mathbf{r}_i^z)^2 (\gamma_i)^{-1}$ ,  $\mathbf{r}^z = [\mathbf{f}_z^T \boldsymbol{\Phi}^{-1/2} \mathbf{A}]$ ,  $\mathbf{r}_i^z$  is the  $i$ th component of  $\mathbf{r}^z$ ;  $\boldsymbol{\omega}_i^t$  denotes the  $i$ th iteration of  $\boldsymbol{\omega}_i$  and the initial iteration  $t$  is 0. Based on the coordinate descent method, an iterative process alternately updates the labels and the weights.

In the next iteration, we calculate the new  $\mathbf{F}$  with new  $\boldsymbol{\omega}$ . The iteration ceases at a given state. After obtaining  $\mathbf{F}$ , we set the  $g$ th class to the  $i$ th data point if the  $g$ th component is the maximum in the  $i$ th row of  $\mathbf{F}$ . A more detailed solution of Equation (9) can be found in Yu, Tao, and Wang (2012).

### 3. Experiments

The experiments were performed with four data sets, including two Airborne Synthetic Aperture Radar (AIRSAR) data sets, a Radarsat-2 data set and an Airborne Visible/Infrared Imaging Spectrometer (AVIRIS) hyperspectral data set. In order to assess the performance of the proposed method with polarization data, we compared our method with the classic SVM, SGL,  $k$ -nearest neighbour ( $k$ -NN) (Duda, Hart, and Stork 2000) and semi-supervised discriminant analysis (SDA) (Cai, He, and Han 2007) classifications. Further, we show the performance for the single-, dual- and full-polarization cases.

### 3.1. Data sets

#### 3.1.1. AIRSAR data

Two PolSAR images acquired by the National Aeronautics and Space Administration Jet Propulsion Laboratory (NASA/JPL) AIRSAR L-band system were downloaded from <http://earth.eo.esa.int/polsarpro/index.html>. One image covers a part in the region of Flevoland in the Netherlands and the other covers an area in San Francisco, California, in the USA.

The image of Flevoland was used for crop classification study. As shown in Figure 1, this image has a size of  $1024 \times 750$  pixels. The pixel size is 6.6 m in the slant range direction and 12.1 m in the azimuth direction. The incidence angles are  $20^\circ$  at near range and  $44^\circ$  at far range. The ground of this image is located at  $52.31^\circ\text{N}$ ,  $5.33^\circ\text{E}$ . Four land-use classes, such as potato, wheat, rape and grass, were extracted, and the samples' amount of each class in our experiment is 500.

The image of San Francisco has a size of  $1024 \times 900$  pixels, as shown in Figure 2. Its incident angles span from  $10^\circ$  to  $60^\circ$ . The ground of this image is located at  $49.13^\circ\text{N}$ ,  $122.45^\circ\text{W}$ , in San Francisco, California, United States. Three land covers, such as vegetation, man-made construction and water, were used for training and testing, and the samples' amount of each class in our experiment is 1000. The two data sets were labelled manually by referring to Lee and Pottier (2009).

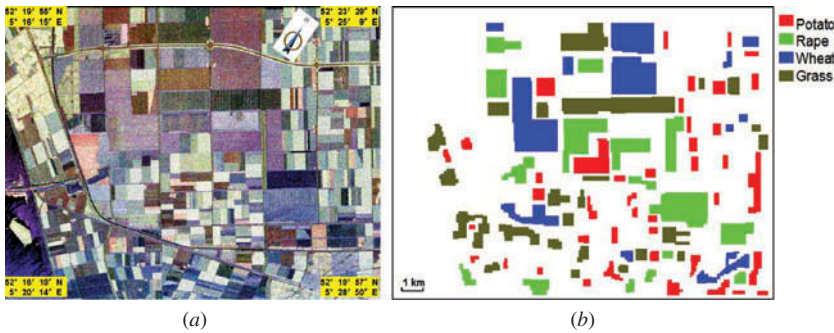


Figure 1. (a) AIRSAR false colour image of Flevoland, based on Pauli decomposition, with  $|S_{hh} + S_{vv}|$  as blue,  $2|S_{hv}|$  as green, and  $|S_{hh} - S_{vv}|$  as red. (b) Training and evaluation polygons.

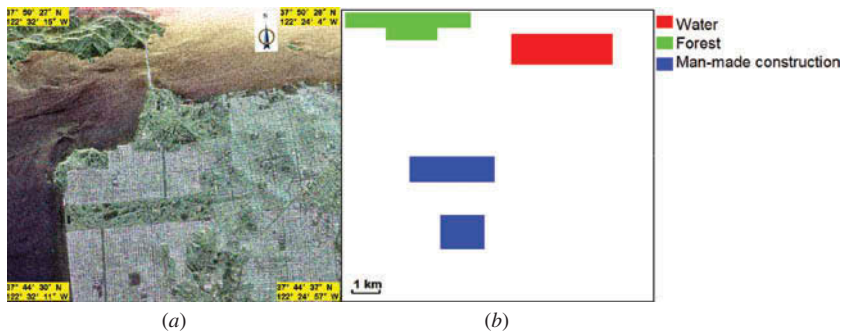


Figure 2. (a) AIRSAR false colour image of San Francisco, based on Pauli decomposition, with  $|S_{hh} + S_{vv}|$  as blue,  $2|S_{hv}|$  as green, and  $|S_{hh} - S_{vv}|$  as red. (b) Training and evaluation polygons.

### 3.1.2. Radarsat-2 data

The third data set, collected by C-band Radarsat-2, is shown in Figure 3. The image has a size of  $2020 \times 13,299$  pixels. The pixel size is 4.87 m in the line-spacing and 4.73 m in the pixel-spacing. The acquisition-start-time is 14:38, 15 April 2008. The beam-mode is Fine Quad-Pol 2. The incidence angles are  $19^\circ$  at near range and  $22^\circ$  at far range. The slant-range-near-edge is 842.87 km. The ground of this image is located at  $49.13^\circ\text{N}$ ,  $123.10^\circ\text{W}$ , in Vancouver, British Columbia, Canada. Four land-cover classes, such as man-made construction, forest, water and low vegetation including bare soil, were selected for training and testing, and the samples' amount of each class in our experiment is 700. The labels were created manually by referring to Google Earth.

### 3.1.3. AVIRIS data

The fourth data set, acquired by an AVIRIS over the Kennedy Space Center, Orlando, Florida, United States, in March 1996, is shown in Figure 4. The image has the size of  $614 \times 512$  pixels. The pixel size is 18 m. There are 224 spectral bands spanning from 400 nm to 2500 nm and 176 bands are used for the study by removing the bands absorbed

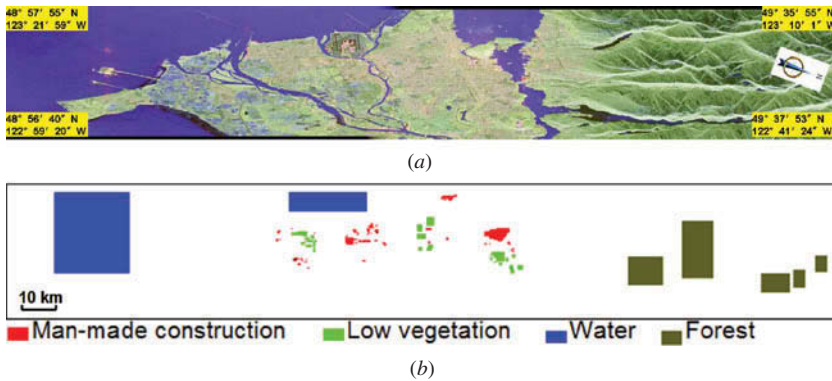


Figure 3. (a) Radarsat-2 false colour image of Vancouver, Canada, based on Pauli decomposition, with  $|S_{hh} + S_{vv}|$  as blue,  $2|S_{hv}|$  as green, and  $|S_{hh} - S_{vv}|$  as red. (b) Training and evaluation polygons.

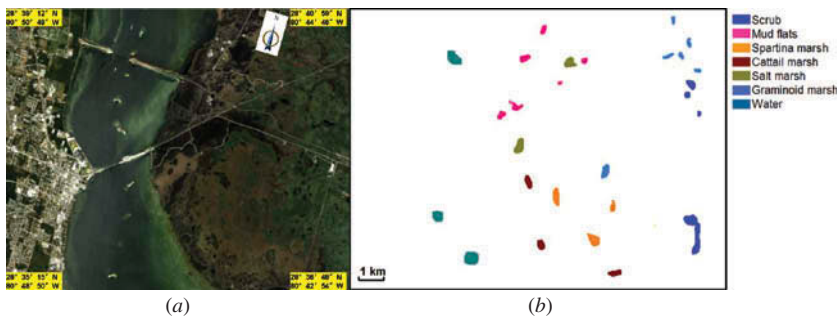


Figure 4. (a) AVIRIS false colour image of Kennedy Space Center, based on Pauli decomposition, with  $|S_{hh} + S_{vv}|$  as blue,  $2|S_{hv}|$  as green, and  $|S_{hh} - S_{vv}|$  as red. (b) Training and evaluation polygons.



by atmospheric moisture and those with low signal-to-noise ratio. Seven land covers are chosen for illustration, including scrub (761 samples), graminoid marsh (503 samples), spartina marsh (520 samples), cattail marsh (404 samples), salt marsh (419 samples), mud flats (431 samples) and water (927 samples). The ground of this image is located at 28.61°N, 80.80°W, in Orlando, United States.

### 3.2. Results

The proposed method was applied to the four data sets. The classification accuracy is given by the mean producer's accuracy (MPA) that represents the mean of the producer's accuracy (expressed in per cent) of several classes. Each testing correct ratio is averaged over 20 trials, and the training data points are randomly extracted from the data sets.

We compared the proposed approach with two supervised classifications: classic SVM and  $k$ -NN, and two semi-supervised classifications: SGL and SDA.

**SVM:** Classic SVM is the most robust and accurate method among all the well-known data mining algorithms, and it has been developed rapidly both in theory and practice. It aims at finding a hyperplane to separate two classes of given samples with a maximal margin. Here, we use it in multiclassification with the library Libsvm written by Chih-Chung Chang and Chih-Jen Lin. The parameters are default.

**SGL:** SGL addresses the pair-wise relationships between any two vertices in the correlated Laplacian graph. We use the regulation, which is similar to the first two items of Equation (9). However, SGL has difficulty tuning the parameters of  $\lambda$  and  $\mu$ . Here, we set  $\lambda$  to be the norm variance of the data points, and  $\mu$  to be  $\lambda/4$ .

**$k$ -NN:** The aim of  $k$ -NN Classification is to locate a group of  $k$  points in the training set that are closest to the labelled point and base the assignment of a label on the labelled point in this neighbourhood. Here,  $k$  is set to be 5.

**SDA:** It aims to find a projection which respects the discriminant structure inferred from the training data. The training data, combined with unlabelled data, are used to build a Laplacian graph which provides a discrete approximation to the local geometry of the data manifold and can be incorporated into objective function. It can preserve the manifold structure.

Figure 5 shows the experiment results for the four data sets based on the proportion of the training data points to all data points, which spanned from 1% to 15%. Our method achieves better performance than that of both SVM and SGL for the four data sets. For SVM, the training data points are too fewer to present the structure of data set. SGL can't take into account high-order information. The MPA of three methods, HGL,  $k$ -NN and SDA, converges to stabilization when the training proportion closes to 5%. HGL achieves better performance than that of  $k$ -NN and SDA for the two AIRSAR data sets, and it is similar for Radarsat-2 data set. However, it is inferior to  $k$ -NN and SDA heavily for AVIRIS data set. And then, we performed the proposed method by tuning the parameters  $\lambda$  and  $\mu$  from 0.1 to 10 in step 0.1. There is a little bit change with different  $\lambda$  and  $\mu$ , and the optimal values are  $\lambda = 1$  and  $\mu = 1$ .

Further, we performed the experiment with full-polarization, dual-polarization and single-polarization. The results, shown in Table 1, indicate that the MPA obtained for the three test data sets for training samples ranges from 5% to 10% for full-polarization, dual-polarization and single-polarization. The first column is the proportion of training data to all data, and the last row is the average MPA. Obviously, the performance of full-polarization exceeds that of dual-polarization, which, because of more information, is better than that of single-polarization. For single-polarization, the overall accuracy of VV-polarization is close to that of HH-polarization.

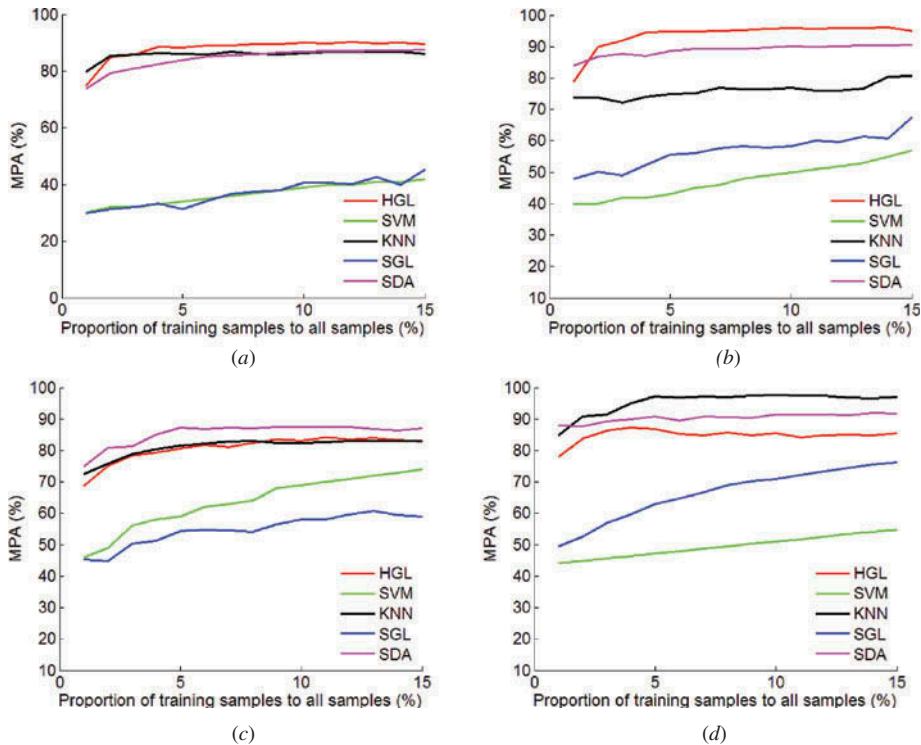


Figure 5. Comparison of HGL to classic SVM, SGL and  $k$ -NN on four data sets of (a) Flevoland, (b) San Francisco, (c) Vancouver, and (d) Kennedy Space Center.

#### 4. Conclusions

This letter addressed the performance of a HGL algorithm for the classification of polarimetric SAR data. We have conducted experiments on four data sets, three PolSAR data sets and a hyperspectral data set. We compared the proposed HGL with classic SVM, SGL,  $k$ -NN and SDA. The proposed algorithm achieves a better overall accuracy than that of SVM, SGL,  $k$ -NN and SDA. Then, a hyperspectral data was conducted on the proposed method. The proposed method could not achieve a better result in this case. Finally, we conducted the experiments with single, dual-, and full-polarization SAR images. The results for full-polarization and dual-polarization are superior to those for single-polarization. The result for full-polarization is much better than that for dual-polarization. Based on our proposed method, we also conclude that the multi-polarization SAR system is superior to single polarization. However, using the proposed method to construct the hypergraph is time-consuming, especially when faced with large data sets. Therefore, in the future, comparable analyses must be performed.

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Table 1. Mean producer's accuracy (MPA) of polarization based on HGL. First row lists the proportion of labelled points to overall samples.

		MPA of HGL (%)																	
		Full PolSAR				Dual PolSAR				Single PolSAR									
		Pauli-decomposition				HH + VV				VV				HH					
Proportion (%)		San Francisco		Vancouver		Flevoland		San Francisco		Vancouver		Flevoland		San Francisco		Vancouver		Flevoland	
		5	95	82	88	79	75	84	62	62	62	62	53	58	51	52	58	58	51
6	95	82	89	82	74	85	63	63	65	59	59	46	56	58	46	48	56		
7	95	83	89	81	75	86	64	64	68	58	58	61	58	61	48	48	58		
8	95	83	90	82	75	86	64	64	69	62	62	48	58	63	48	48	58		
9	96	82	90	83	74	85	65	65	69	62	62	65	61	66	65	65	61		
10	96	83	90	82	74	86	64	64	70	62	62	65	60	66	65	65	60		
Average	95.3	82.5	89.3	81.5	74.5	85.3	63.7	63.7	67.2	59.3	59.3	55	57.3	61	55	55	57.3		

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